Area Under the Curve

1. Area of the region bounded by the curve $y = e^x$ and the lines x=0 and y=e is

a) e-1 b)
$$\int_{1}^{e} \log(e+1-y) dy$$
 c) $e - \int_{0}^{1} e^{x} dx$ d) $\int_{0}^{e} \log y dy$

2. Sketch the region bounded by the curves $y = x^2$ and $y = \frac{2}{1+x^2}$. Find its area. 2

Ans:
$$\pi - \frac{2}{3}$$

3. Sketch the region bounded by the curves $y = \sqrt{5-x^2}$ and y = |x-1| and find its area. Ans: $\frac{5\pi}{4} - \frac{1}{2}$

4. Find the area bounded by the x-axis, part of the curve $y = \left(1 + \frac{8}{x^2}\right)$ and the

ordinates x=2 and x=4. Ans: 4

5. Show that the area bounded by the curve $y = 2x - x^2$ and the straight line $y = 2x - x^2$ and the straight line

$$y = -x$$
 is $\frac{y}{2}$ sq.unit

6. Find the area bounded by the curves y = x - 1 and $(y - 1)^2 = 4(x + 1)$. Ans: $\frac{64}{2} sa unit$

$$\frac{64}{3}$$
 sq.unit

- 7. Find the area enclosed by the parabola $y^2 = 2x$ and the two tangents drawn at the points (2,2) and (2,-2).
- 8. Find the area enclosed by the curve |x|+|y|=1.
- 9. Find the area enclosed between the curves $y = e^{-x}$, $y = \log_e(x+e)$ and the x-axis. Ans: 2 sq.units
- 10. Find the area bounded by the curves |x| + |y| = 1 and y = |x|.

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